



# Double-beta decay: to quench or not to quench

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### Classical Double Beta Decay Problem

Z+1

 $0^{+}$ 

2<sup>+</sup>

Z+2







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## The Nobel Prize in Physics 2015



Photo © Takaaki Kajita Takaaki Kajita Prize share: 1/2



Photo: K. McFarlane. Queen's University /SNOLAB

Arthur B. McDonald Prize share: 1/2

The Nobel Prize in Physics 2015 was awarded jointly to Takaaki Kajita and Arthur B. McDonald *"for the discovery of neutrino* TRIUMF DI oscillations, which shows that neutrinos have mass" 12, 2016







### Neutrinoless Double Beta Decay



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## Neutrino $\beta\beta$ effective mass

#### arxiv:1507.08204

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$$\left\langle m_{\beta\beta} \right\rangle = \left| \sum_{k=1}^{5} m_{k} U_{ek}^{2} \right| = \left| c_{12}^{2} c_{13}^{2} m_{1} + c_{13}^{2} s_{12}^{2} m_{2} e^{i\phi_{2}} + s_{13}^{2} m_{3} e^{i\phi_{3}} \right| \qquad \Leftarrow T_{1/2}^{-1}(0v) = G^{0v}(Q_{\beta\beta}) \left[ M^{0v}(0^{+}) \right]^{2} \left( \frac{\langle m_{\beta\beta} \rangle}{m_{e}} \right)^{2}$$

$$\phi_2 = \alpha_2 - \alpha_1 \qquad \phi_3 = -\alpha_1 - 2\delta$$

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### Neutrinoless Double Beta Decay Black Box



$$\left[T_{1/2}^{0\nu}\right]^{-1} = G^{0\nu} \left|\sum_{j} M_{j} \eta_{j}\right|^{2} = G^{0\nu} \left|M^{(0\nu)} \eta_{\nu L} + M^{(0N)} (\eta_{NL} + \eta_{NR}) + \tilde{X}_{\lambda} \right| < \lambda > + \tilde{X}_{\eta} < \eta > + M^{(0\lambda')} \eta_{\lambda'} + M^{(0\tilde{q})} \eta_{\tilde{q}} + \cdots \right|^{2}$$

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### Low-energy LR contributions to $0\nu\beta\beta$ decay





Low-energy effective Hamiltonian

$$\mathcal{H}_W = \frac{G_F}{\sqrt{2}} j_L^\mu J_{L\mu}^+ + h.c.$$

 $j_{L/R}^{\mu} = \overline{e} \gamma^{\mu} (1 \mp \gamma^5) v_e$ 



(b)

(d)

 $\mathcal{H}_{W} = \frac{G_{F}}{\sqrt{2}} \Big[ j_{L}^{\mu} \Big( J_{L\mu}^{+} + \kappa J_{R\mu}^{+} \Big) + j_{R}^{\mu} \Big( \eta J_{L\mu}^{+} + \lambda J_{R\mu}^{+} \Big) \Big] + h.c.$ Left – right symmetric model



(e)

 $-\mathcal{L} \supset \frac{1}{2} h_{\alpha\beta}^{T} \left( \overline{v}_{\beta L} \ \overline{e}_{\alpha L} \right) \begin{pmatrix} \Delta^{-} & -\Delta^{0} \\ \Delta^{--} & \Delta^{-} \end{pmatrix} \begin{pmatrix} e_{R}^{c} \\ -v_{R}^{c} \end{pmatrix} + hc$ 

No neutrino exchange



(a)

(c)







### More long-range contributions?

SUSY / w R – parity violation : e.g. Rep. Prog. Phys. 75, 106301(2012)

Hadronization /w R-parity v. and heavy neutrino



$$\left[T_{1/2}^{0\nu}\right]^{-1} = G^{0\nu} \left|\sum_{j} M_{j} \eta_{j}\right|^{2} = G^{0\nu} \left|M^{(0\nu)} \eta_{\nu L} + M^{(0N)} (\eta_{NL} + \eta_{NR}) + \tilde{X}_{\lambda} < \lambda > + \tilde{X}_{\eta} < \eta > + M^{(0\lambda')} \eta_{\lambda'} + M^{(0\tilde{q})} \eta_{\tilde{q}} + \cdots \right|^{2}$$

(i)  $\eta_{NL}$  negligible in most models; (ii)  $\langle \eta \rangle \& \langle \lambda \rangle$  ruled in /out by energy or angular distributions

$$\left[T_{1/2}^{0\nu}\right]^{-1} \cong G^{0\nu} \left| M^{(0\nu)} \eta_{\nu L} + M^{(0N)} \eta_{NR} \right|^2 \approx G^{0\nu} \left[ \left| M^{(0\nu)} \right|^2 \left| \eta_{\nu L} \right|^2 + \left| M^{(0N)} \right|^2 \left| \eta_{NR} \right|^2 \right]$$
 No interference terms!

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$$r(\nu/N) = T_{1/2}^{\nu/N}(1)/T_{1/2}^{\nu/N}(2) = \frac{G_{01}^{0\nu}(2) \left| M^{0\nu/N}(2) \right|^2}{G_{01}^{0\nu}(1) \left| M^{0\nu/N}(1) \right|^2}$$

	Ge/Se		Ge/Te		Ge/Xe		Se/Te		Se/Xe		Te/Xe	
	Ge	Se	Ge	Те	Ge	Xe	Se	Те	Se	Xe	Те	Xe
$\overline{G_{01}^{0\nu} \times 10^{14}}$	0.237	1.018	0.237	1.425	0.237	1.462	1.018	1.425	1.018	1.462	1.425	1.462
$M^{0\nu}(1/2)$	3.57	3.39	3.57	1.93	3.57	1.76	3.39	1.93	3.39	1.76	1.93	1.76
$M^{0N}(1/2)$	202	187	202	136	202	143	187	136	187	143	136	143
$T_{1/2}^{\nu}(1)/T_{1/2}^{\nu}(2)$	3.	87	1.	76	1.	50	0.4	45	0.	39	0.8	85
$T_{1/2}^N(1)/T_{1/2}^N(2)$	3.	68	2.	73	3.	09	0.	74	0.	84	1.1	13
$R(N/\nu)$ present	$\left  \begin{array}{c} 0. \end{array} \right $	95	1.	55	2.	06	1.	63	$\boxed{\qquad 2.}$	17	1.3	33
$\overline{R(N/\nu) \ [45]}$	1.	02	1.	39	1.4	42	1.	36	1.	39	1.(	)3

R(N / v) = r(N) / r(v)

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 $p_{3/2}$ 

 $f_{7/2}$ 

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0.02

0 <u>∟</u> 0

2

6

4

8

E<sub>x</sub> (MeV)

10

12

14

G



Α<sub>Y</sub> Z+2

Ϋ́Τ Z+1

 $E_0 = \frac{1}{2}Q_{\beta\beta} + \Delta M \left( {}^A_{Z+1}T - {}^A_Z X \right)$ 

### 2v Double Beta Decay (DBD) of <sup>48</sup>Ca

$$T_{1/2}^{-1} = G^{2\nu}(Q_{\beta\beta}) \Big[ M_{GT}^{2\nu}(0^{+}) \Big]^{2}$$

$$M_{GT}^{2\nu}(0^{+}) = \sum_{k} \frac{\langle 0_{f} \| \sigma \tau^{-} \| 1_{k}^{+} \rangle \langle 1_{k}^{+} \| \sigma \tau^{-} \| 0_{i} \rangle}{E_{k} + E_{0}}$$

$$\overset{48}{} Ca \xrightarrow{2\nu \beta\beta} \overset{48}{} Ti$$
The choice of valence space is important!?
$$B(GT) = \frac{\left| \langle f \| \sigma \cdot \tau \| i \rangle \right|^{2}}{(2J_{i} + 1)}$$

$$\overset{ISR}{=} \frac{48Ca}{f_{5/2}} \frac{48Ti}{f_{5/2}}$$

$$\overset{Ikeda satisfied in pf !}{=} \frac{P_{1/2}}{f_{5/2}}$$

$$\overset{012}{=} \frac{\int_{0}^{006}}{\int_{0}^{006}} \frac{1}{f_{5/2}} \frac{1}{f_{5/2}} \int_{0}^{006}}{\int_{0}^{006}} \frac{1}{f_{5/2}} \int_{0}^{006}}{\int_{0}^{006}} \frac{1}{f_{5/2}} \int_{0}^{006}} \frac{1}{f_{5/2}} \int_{0}^{006}}{\int_{0}^{006}} \frac{1}{f_{5/2}} \int_{0}^{006} \int_{0}^{006} \frac{1}{f_{5/2}} \int_{0}^{006}}{\int_{0}^{006}} \frac{1}{f_{5/2}} \int_{0}^{006} \int_{0}^{006} \frac{1}{f_{5/2}} \int_{0}^{0} \frac{1}{f_{5/2}} \int_{0$$

 $\rightarrow Z - 1) = 3(N - Z)$  $\rightarrow 0.74 g_A \sigma \tau$ 

Horoi, Stoica, Brown, PRC 75, 034303 (2007)





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......

M(GT) USDB

M(GT) USDA

M(GT) USD

1

0

-----

theory-fit

2

3





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## The g<sub>A</sub> problem

#### PHYSICAL REVIEW C 87, 014315 (2013)



#### Phys. Lett. B 711, 62 (2012)

#### Table 2

The ISM predictions for the matrix element of several  $2\nu$  double beta decays (in MeV<sup>-1</sup>). See text for the definitions of the valence spaces and interactions.

	$M^{2\nu}(exp)$	q	$M^{2\nu}(th)$	INT
$^{48}$ Ca $\rightarrow ^{48}$ Ti	$0.047\pm0.003$	0.74	0.047	kb3
$^{48}$ Ca $\rightarrow ^{48}$ Ti	$0.047\pm0.003$	0.74	0.048	kb3g
$^{48}$ Ca $\rightarrow ^{48}$ Ti	$0.047\pm0.003$	0.74	0.065	gxpf1
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140\pm0.005$	0.60	0.116	gcn28:50
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140\pm0.005$	0.60	0.120	jun45
$^{82}\text{Se} \rightarrow {}^{82}\text{Kr}$	$0.098\pm0.004$	0.60	0.126	gcn28:50
$^{82}$ Se $\rightarrow {}^{82}$ Kr	$0.098\pm0.004$	0.60	0.124	jun45
$^{128}\text{Te} \rightarrow ^{128}\text{Xe}$	$0.049\pm0.006$	0.57	0.059	gcn50:82
$^{130}$ Te $\rightarrow ^{130}$ Xe	$0.034\pm0.003$	0.57	0.043	gcn50:82
$^{136}$ Xe $\rightarrow ^{136}$ Ba	$0.019\pm0.002$	0.45	0.025	gcn50:82

FIG. 13. (Color online) Value of  $g_{A,eff}$  extracted from experiment for IBM-2 and the ISM.

 $G^{2\nu}, G^{0\nu} \propto g_A^4$ 









## The g<sub>A</sub> problem

#### $q_{\mathrm{exp}}$



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## The g<sub>A</sub> problem

#### $q_{\mathrm{exp}}$



#### Physics Letters B 711 (2012) 62-64

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Closure Approximation and Beyond in Shell Model

$$M_{S}^{0v} = \sum_{\substack{j, p < p' \\ n < n' \\ p < n}} (\Gamma) \left\langle \overline{0_{f}^{+} \left[ \left( a_{p}^{+} a_{p'}^{+} \right)^{g} \left( \tilde{a}_{n}, \tilde{a}_{n} \right)^{g} \right]^{0}} \left| 0_{i}^{+} \right\rangle \left\langle p p'; \mathcal{I} \right| \int q^{2} dq \left[ \hat{S} \frac{h(q) j_{\kappa}(qr) G_{FS}^{2} f_{SRC}^{2}}{q(q + \langle E \rangle)} \tau_{1-} \tau_{2-} \right] \left| n n'; \mathcal{I} \right\rangle - closure$$

$$M_{S}^{0v} = \sum_{\substack{pp' nn' \\ J & g'}} (\tilde{\Gamma}) \left\langle 0_{f}^{+} \left\| \left( a_{p}^{+} \tilde{a}_{n} \right)^{J} \right\| \mathcal{I}_{k} \right\rangle \left\langle \mathcal{I}_{k} \left\| \left( a_{p'}^{+} \tilde{a}_{n'} \right)^{J} \right\| 0_{i}^{+} \right\rangle \left\langle p p'; \mathcal{I} \right| \int q^{2} dq \left[ \hat{S} \frac{h(q) j_{\kappa}(qr) G_{FS}^{2} f_{SRC}^{2}}{q(q + \langle E \rangle)} \tau_{1-} \tau_{2-} \right] \left| n n'; \mathcal{I} \right\rangle - beyond$$

Challenge: there are about 100,000  $J_k$  states in the sum for 48Ca

Much more intermediate states for heavier nuclei, such as <sup>76</sup>Ge!!!

 $M^{0\nu} = M_{GT}^{0\nu} - (g_V / g_A)^2 M_F^{0\nu} + M_T^{0\nu}$  $\hat{S} = \begin{cases} \sigma_1 \tau_1 \sigma_2 \tau_2 & Gamow - Teller (GT) \\ \tau_1 \tau_2 & Fermi (F) \\ [3(\vec{\sigma}_1 \cdot \hat{n})(\vec{\sigma}_2 \cdot \hat{n}) - (\vec{\sigma}_1 \cdot \vec{\sigma}_2)] \tau_1 \tau_2 & Tensor (T) \\ TRIUMF DBDW May \\ 12, 2016 \end{cases}$ 

No-closure may need states out of the model space (not considered).

#### **Minimal model spaces**

- $^{82}$ Se : 10M states
- <sup>130</sup>Te : 22M states
- <sup>76</sup>Ge: 150M states





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ISM-Men J. Menéndez, A. Poves, E. Caurier, F. Nowacki, NPA 818 139–151 (2009).

SM M. Horoi et. al. PRC 88, 064312 (2013), PRC 89, 045502 (2014), PRC 89, 054304 (2014), PRC 90, 051301(R) (2014), PRC

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**91**, 024309 (2015), PRL **110**, 222502 (2013), PRL **113**, 262501(2014).

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**IBA-2** J. Barea, J. Kotila, and F. Iachello, Phys. Rev. C 87, 014315 (2013).

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QRPA-Jy J. Hivarynen and J. Suhonen, PRC 91, 024613 (2015), ISM-StMa J. Menendez, private communication.

ISM-CMU M. Horoi et. al. PRC 88, 064312 (2013), PRC 90, PRC 89, 054304 (2014), PRC 91, 024309 (2015), PRL 110, 222502 (2013).

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### The effect of larger model spaces for <sup>48</sup>Ca



#### See also PRL 116, 112502 (2016)

<b>M(0v)</b>	SDPFU	SDPFMUP
0 ħω	0.941	(0.623)
$0+2\hbar\omega$	1.182 (26%)	1.004 (61%)

SDPFU: PRC 79, 014310 (2009)

SDPFMUP: PRC 86, 051301(R) (2012)



	<b>M(0v)</b>
$0 \hbar \omega / \text{GXPF1A}$	0.733
$0 \hbar \omega + 2^{nd}$ ord./GXPF1A	1.301 (77%)

arXiv:1308.3815, PRC 89, 045502 (2014)

PRC 87, 064315 (2013)







## Towards an effective 0vDBD operator

SRG evolution

 $H_{\lambda} = U_{\lambda} H_{\lambda = \infty} U_{\lambda}^{\dagger}$ 

$$rac{dH_\lambda}{d\lambda} = -rac{4}{\lambda^5}[[G,H_\lambda],H_\lambda]$$

$$O_{\lambda} = U_{\lambda}O_{\lambda=\infty}U_{\lambda}^{+}$$



#### N3LO 500

arXiv:1302.5473



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$$O_{\lambda} = U_{\lambda}O_{\lambda=\infty}U_{\lambda}^{+}$$



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 $^{76}$ Ge



### 懗 CENTRAL MICHIGAN Towards an effective 0vDBD operator: heavy neutrino-exchange NME

$$O_{\lambda} = U_{\lambda}O_{\lambda=\infty}U_{\lambda}^{+}$$



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## CENTRAL MICHIGAN Towards an effective 0vDBD operator: light neutrino-exchange NME





SciDAC Scientific Discovery Minister Consultation

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## Observation of $0\nu\beta\beta$ will signal New Physics Beyond the Standard Model.

Black box theorem (all flavors + oscillations)



(i) Neutrinos are Majorana fermions.

 $0\nu\beta\beta$  observed  $\Leftrightarrow$  at some level

(ii) Lepton number conservation is violated by 2 units

$$(iii) \ \left\langle m_{\beta\beta} \right\rangle = \left| \sum_{k=1}^{3} m_{k} U_{ek}^{2} \right| = \left| c_{12}^{2} c_{13}^{2} m_{1} + c_{13}^{2} s_{12}^{2} m_{2} e^{i\phi_{2}} + s_{13}^{2} m_{3} e^{i\phi_{3}} \right| > 0$$

Regardless of the dominant  $0\nu\beta\beta$  mechanism!

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## Collaborators:

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- Roman Senkov, CUNY
- Andrei Neacsu, CMU
- Jonathan Engel, UNC
- Jason Holt, TRIUMF
- Petr Navratil, TRIUMF
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